

Advanced course on

HIGH RESOLUTION ELECTRONIC MEASUREMENTS IN NANO-BIO SCIENCE



Measurements at a given frequency The Lock-in concept

Marco Sampietro

Small bandwidth \Rightarrow **Low noise**



... small bandwidth at high frequency



Marco Sampietro

Example : measurement of R





The Lock-in concept 20 min

Performance in sensitivity 20 min

The lock-in concept

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The LOCK-IN idea



The LOCK-IN idea



Credited to Robert Dicke, founder of Princeton Applied Research (PAR) in the 1960's.

The lock-in concept

Tracking sensor with the LOCK-IN



DUT variations can be tracked with time by simply monitoring the level of the output

Phase selectivity of the Lock-in



Frequency selectivity of the Lock-in



Signals with different frequency to reference are rejected

The	lock-in	concept
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Noise suppression



The lock-in concept

Analytical view - Signal



Analytical view - Power



The lock-in concept

Signal to Noise RATIO



Lock-In Noise Filtering



- The modulation *whiten* the noise spectrum in base band at the value sampled at f₀
- The order of the filter is not critical for the noise (a first order is ok even with non-white noise)
- The filter has to properly cut the 2f₀ component



M. Carminati et al. "Attofarad resolution potentiostat for electrochemical measurements on nanoscale biomolecular interfacial systems.," Rev. Sci. Instrum., vol. 80, no. 12, p. 124701 (2009), doi: 10.1063/1.3245343.



- The Lock-in concept 20 min

Performance in sensitivity 20 min

The lock-in concept

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Limit of sensitivity : Noise Analysis

A recap of the input noise of the TIA :



 $S_{i} = \overline{i_{n}^{2}} + 4kT(G_{x} + G_{f}) + \overline{e_{n}^{2}}\omega^{2}(C_{x} + C_{p})^{2} + \overline{e_{n}^{2}}(G_{x} + G_{f})^{2}$ To be compared with the Signal (V, I)

Limit of sensitivity - for R



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Limit of sensitivity - for R



Sinusoidal measurement of C



Limit of sensitivity - for C



Limit of sensitivity - for C



Improvement with Voltage amplitude







Special TIA for square wave mixer



If a square wave mixer is used, it introduces harmonics that fold a lot of noise If a square wave mixer is used, higher harmonics give little noise



In conclusion ...

The lock-in concept

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A Lock-in amplifier is «like» a band-pass filter at f₀



By changing measurement frequency f_0 , you can choose the optimal position

Things to remember (2)



Signal variations can be tracked with time by simply monitoring the level of the output

Extremely high sensitivity can be reached in device characterisation

